

Shri Swami Vivekanand Shikshan Sanstha's

Vivekanand College, Kolhapur (Empowered Autonomous).

Department of Physics

Date: 02/09/2024

Internal Examination Notice

The students of B.Sc. I, II and III are hereby informed that the internal examination of current semester is scheduled as per following time table:

Sr. No.	Class and Sem	Paper No.	Title of the paper	Date and time
1.	B.Sc. I, SEM I	I	Mechanics I	24/09/2024 10: 00 to 11:00 am
2.	B.Sc. I, SEM I	II	Electricity and Magnetism I	25/09/2024 10: 00 to 11:00 am
3.	B.Sc. II, SEM III	V	Thermal and statistical mechanics I	24/09/2024 10: 00 to 11:00 am
4.	B.Sc. II, SEM III	VI	Waves and Oscillations	25/09/2024 10: 00 to 11:00 am
5.	B.Sc. III, SEM V	IX	Mathematical Physics	24/09/2024 12:00 to 01:00 pm
6.	B.Sc. III, SEM V	X	Nuclear and Particle Physics	25/09/2024 12:00 to 01:00 pm
7.	B.Sc. III, SEM V	XI	Quantum physics	26/09/2024 12:00 to 01:00 pm
8.	B.Sc. III, SEM V	XII	Solid state physics I	27/09/2024 12:00 to 01:00 pm

Nature of question paper

- For B.Sc. I and II

Total Marks (for each paper) = 10

Q: 1) Select correct alternative

(4 marks)

Q: 2) Short answer question (any two out of three)

(08 marks)

- For B.Sc. III

Total Marks (for each paper) = 15

Q: 1) Select correct alternative

(3 marks)

Q: 2) Short answer question (any three out of four)

(12 marks)



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HEAD
DEPARTMENT OF PHYSICS
VIVEKANAND COLLEGE, KOLHAPUR
(EMPOWERED AUTONOMOUS)

Shri Swami Vivekanand Shikshan Sanstha, Kolhapur's

Vivekanand College, Kolhapur

(Empowered Autonomous)

Department of Physics

Date: 24/09/2024

B. Sc. / M/Sc. Part - I, Semester - I, PHYSICS Paper - I

Title of the Paper: Mechanics - I

Name of Teacher: Dr. Gumanjya I. Inamdar

Internal Examination Attendance Sheet

Sr. No.	Name of the Student	Paper I 24/9/2024	Paper II 25/09/2024			
1)	Shivali Shivaji Kumbhar	<u>Shk</u>	<u>Shk</u>			
2)	Amsuta Vikeant Malawade	<u>Malawade</u>	<u>Malawade</u>			
3)	Sanika Shivaji Chougale	<u>Chougale</u>	<u>Chougale</u>			
4)	Samrudhik Kishnat Powar	<u>Powar</u>	<u>Powar</u>			
5)	Vaishnavi S. Chougale	<u>V. Chougale</u>	<u>V. Chougale</u>			
6)	Mrunali I. Kotmire	<u>Kotmire</u>	<u>Kotmire</u>			
7)	Shreya S. Patil	<u>Patil</u>	<u>Patil</u>			
8)	Grishma S. Tiipankar	<u>Tiipankar</u>	<u>Tiipankar</u>			
9)	Megha S. Patil	<u>M. Patil</u>	<u>M. Patil</u>			
10)	Shreya P. Powar	<u>Powar</u>	<u>Powar</u>			
11)	Anushka J. Patil	<u>Patil</u>	<u>Patil</u>			
12)	PRANALI R. GATKWARD	<u>Gatkward</u>	<u>Gatkward</u>			
13)	Vaishnavi S. Sawal	<u>Sawal</u>	<u>Sawal</u>			
14)	Shrushti S. Chougale	<u>S.S.C</u>	<u>S.S.C</u>			
15)	Anuja M. Matlawade	<u>Anuja</u>	<u>Anuja</u>			
16)	Nandini R. Chorage	<u>Chorage</u>	<u>Chorage</u>			
17)	Purva D. Chougale	<u>Purva</u>	<u>Purva</u>			
18)	Gungun V. Dhanwani	<u>Dhanwani</u>	<u>Dhanwani</u>			
19)	Jaykta Jaykward	<u>Jaykward</u>	<u>Jaykward</u>			
20)	Sakshi Chougale	<u>Chougale</u>	<u>Chougale</u>			



21)	Diksha. V. Sutar	<u>Diksha</u>	<u>Diksha</u>
22)	Pratiksha. R. Mohite	<u>Pratiksha</u>	<u>Pratiksha</u>
23)	Anushka B. Powar	<u>Anushka</u>	<u>Anushka</u>
24)	Sakshi. D. Sakhedkar	<u>Sakshi</u>	<u>Sakshi</u>
25)	Sneha. P. Murgude	<u>Sneha</u>	<u>Sneha</u>
26)	Trupti D. Chougale	<u>Trupti</u>	<u>Trupti</u>
27)	Prati K. Maruda	<u>Prati</u>	<u>Prati</u>
28)	Sanika S. Barade	<u>Sanika</u>	<u>Sanika</u>
29)	Samruddhi. S. Dixit	<u>Samruddhi</u>	<u>Samruddhi</u>
30)	Aditi S. Kumbhar	<u>Aditi</u>	<u>Aditi</u>
31)	Shruti A. Sutar	<u>S.A. Sutar</u>	<u>S.A. Sutar</u>
32)	Aspita. B. Patil	<u>A.B. Patil</u>	<u>A.B. Patil</u>
33)	Pratiksha. P. Patil	<u>P. Patil</u>	<u>P. Patil</u>
34)	Sai Sarjerao Navale	<u>SNavale</u>	<u>SNavale</u>
35)	Jiya Salim Mulla	<u>Jmulla</u>	<u>Jmulla</u>
36)	Swaleha pathan	<u>Swaleha</u>	<u>Swaleha</u>
37)	Sahil S. Kumbhar	<u>Sahil</u>	<u>Sahil</u>
38)	Shubham D. Daver	<u>S.Daver</u>	<u>S.Daver</u>
39)	Hrushvaudhan. Kate	<u>H.Kate</u>	<u>H.Kate</u>
40)	Rushi. Umesh. Pawar	<u>Rushi</u>	<u>Rushi</u>
41)	Sahil Sachin Pachatkar	<u>S.P</u>	<u>S.P</u>
42)	Abhay Nivas Patil	<u>A.Patil</u>	<u>A.Patil</u>
43)	Pranav Deshrath Patil	<u>Patil</u>	<u>Patil</u>
44)	Mayuresh A. Thunkikar	<u>M</u>	<u>M</u>
45)	Ayan S. Shaikh	<u>A.S.S</u>	<u>A.S.S</u>
46)	Tejas. P. Patil	<u>T.Patil</u>	<u>T.Patil</u>
47)	Abhishek. S. Parale	<u>A</u>	<u>A</u>
48)	Yash. L. Dhotre	<u>Y.Dhotre</u>	<u>Y.Dhotre</u>
49)	Mukund P. Mhetre	<u>M</u>	<u>M</u>



Shri Swami Vivekanand Shikshan Sanstha, Kolhapur's

Vivekanand College, Kolhapur

(Empowered Autonomous)

Department of Physics

B. Sc. / M.Sc. Part - I, Semester - I, PHYSICS Paper - I

Title of the Paper: Mechanics I

Name of Teacher: Dr. Sumayya T. Inamdar

Attendance Sheet

Sr. No.	Name of the Student	Paper I 24/09/2024	Paper II 25/09/2024		
1)	SHREYASH. S. SHINGATE	S.S.Shingate	S.S.Shingate		
2)	Samarth . B. Koli	S.B.Koli	S.B.Koli		
3)	Harshavardhan B. Chavan	H.B.Chavan	H.B.Chavan		
4)	Mahesh Gawari	M.G.			
5)	Suyash . D. Ghugare	S.G.			
6)	Shivtej. v. Patil	S.Patil			
7)	Atharva R. Patil	A.R.Patil			
8)	Shivam P. Bodake	S.B.			
9)	Adarsh . R. Jha	A.R.Jha			
10)	Parth. P. Gavali	P.P.G			
11)	Poojaal S. Lokhande	P.L.			
12)	Atharv . M. Salokhe	A.S.			
13)	Pramod . P. Khot	P.K.			
14)	Nikhil . S. Salokhe	N.S.			
15)	Parth. V. Patil	P.V.P.			
16)	Amit . S. Patil	A.S.Patil			
17)	Pandurang Rupnar	P.R. Rupnar			
18)	Vinit N. Magdum	V.N.M.			
19)	Sures . D. Yelpare	S.D.Y.			
20)	Alfaj R. Patel	A.R.Patel			



21)	Mahamadsaad G. Pendhari	<u>Pradeep</u>	<u>Pradeep</u>
22)	Parth yashwant mali.	<u>Pradeep</u>	<u>Pradeep</u>
23)	Harsh V. Pawar	<u>Harsh</u>	<u>Harsh</u>
24)	Shubham S. Devpuje	<u>SSP</u>	<u>SSP</u>
25)	Paras . P. Thakare	<u>Pradeep</u>	
26)	Dinosh . D. Mane	<u>Mane</u>	<u>Mane</u>
27)	Jiya Salim Mulla	Jmulla	Jmulla
28)	Prathamesh S. kumbhar	<u>Pradeep</u>	<u>Pradeep</u>
29)			
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"Education for Knowledge, Science and Culture"
-Shikshanmaharshi Dr. Bapuji Salunkhe
Shri Swami Vivekanand Shikshan Sanstha, Kolhapur

Vivekanand College, Kolhapur (Empowered Autonomous).

Department of Physics

B.Sc. Part-I SEM I Examination (2024-25)

Electricity and Magnetism I

Paper II (Paper code: DSC03PHY12)

Date :

Total Marks: 10

Day :

Time :-

Instructions:-

- 1) All questions are compulsory.
- 2) Figures to the right indicate full marks.
- 3) Use of log table and calculator is allowed.

Q.1) Select correct alternative

(2)

1. The gradient of scalar function $(\nabla \cdot \phi)$ is -----
(a) a vector (b) a scalar
(c) used to represent equipotential surface (d) always zero
2. If magnitude of $\vec{A} \times \vec{B} = AB$, then the two vectors must be -----
(a) parallel to each other (b) antiparallel to each other
(c) inclined at an angle 45° with each other (d) always antiparallel

Q.2 Attempt any TWO

(08)

1. Define scalar product of two vectors. State its characteristics.
2. Explain the physical significance of gradient of scalar function $(\nabla \cdot \phi)$.
3. Write a short note divergence of vector field $\vec{\nabla} \cdot \vec{V}$.



Name - Sai Sarjendra Navale

॥ ज्ञान, विज्ञान आणि सुसंस्कार यांसाठी शिक्षण प्रसार ॥

- शिक्षणमहर्षी डॉ. बापूजी साळुंखे

Shri Swami Vivekanand Shikshan Sanstha Kolhapur's

51457

VIVEKANAND COLLEGE, KOLHAPUR (AUTONOMOUS)

SUPPLIMENT

Date - 25-09-2024

Suppliment No. :

Roll No. : 7253

Class : BSc (I)

Signature
of
Supervisor

Subject : Physics (Electricity & magnetism)
(Internal)

Test / Tutorial No. :

Div. :

10/10 *Jeet*

Q1)

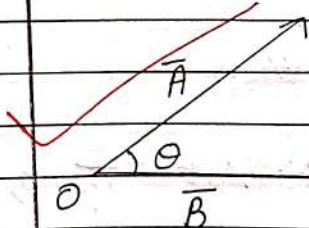
1) (a) a Vector.

2) If magnitude of $\vec{A} \times \vec{B} = AB$, then two vectors must be perpendicular. * (All options are different).

Q2)

1) Scalar product -

The scalar product is also called as dot product is a product of two vectors & cosine angle between them.



If A & B are two vectors then their scalar product is given as,
 $\vec{A} \cdot \vec{B} = AB \cos \theta$

* Characteristics of scalar product.

1) The scalar product or dot product obeys commutative law.

i.e if A & B are two vectors then,

P.T.O



$$A \cdot B = B \cdot A$$

[2] Scalar product also obeys distributive law
i.e. $A \cdot (B + C) = A \cdot B + A \cdot C$

[3] Scalar product obeys associative law,
 $A \cdot (B + C) = (A + B) \cdot C$

[4] The scalar product of A & B depends upon an angle made by two vectors.

(1) If $\theta = 0$,

$$A \cdot B = AB \cos 0 = AB$$

(Hence, scalar product is maximum)

(2) If $\theta = 90^\circ$,

$$A \cdot B = AB \cos 90^\circ = 0$$

(Scalar product is 0)

(3) If $\theta = 180^\circ$,

$$A \cdot B = AB \cos 180^\circ = -AB$$

(Scalar product is minimum)

[5] If two vectors are parallel then,

$$\hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1$$

And, if two vectors are perpendicular then,

$$\hat{i} \cdot \hat{j} = \hat{j} \cdot \hat{k} = \hat{i} \cdot \hat{k} = 0$$

[6] If A & B are two vectors such that,

$$A = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

$$B = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$$

Then.

$$A \cdot B = (A_x \hat{i} + A_y \hat{j} + A_z \hat{k}) \cdot (B_x \hat{i} + B_y \hat{j} + B_z \hat{k})$$

$$= A_x B_x (\hat{i} \cdot \hat{i}) + A_x B_y (\hat{i} \cdot \hat{j}) + A_x B_z (\hat{i} \cdot \hat{k}) \\ + A_y B_x (\hat{j} \cdot \hat{i}) + A_y B_y (\hat{j} \cdot \hat{j}) + A_y B_z (\hat{j} \cdot \hat{k}) \\ + A_z B_x (\hat{k} \cdot \hat{i}) + A_z B_y (\hat{k} \cdot \hat{j}) + A_z B_z (\hat{k} \cdot \hat{k})$$

$$= A_x B_x + 0 + 0 + 0 + A_y B_y + 0 + 0 + 0 + A_z B_z$$

$$A \cdot B = A_x B_x + A_y B_y + A_z B_z \quad \begin{matrix} \dots (\hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1) \\ (\hat{i} \cdot \hat{j} = \hat{j} \cdot \hat{i} = \hat{i} \cdot \hat{k} = \hat{k} \cdot \hat{i} = 0) \end{matrix}$$

- 3) 11 The divergence of vector field $\vec{\nabla} \cdot \vec{v}$ is a scalar quantity which can be expressed in the form of.

$$\vec{\nabla} \cdot \vec{v} = \left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} \right)$$

- 12 Here, v_x, v_y & v_z are vectors & $\vec{\nabla}$ is a del operator or differential operator.

$$\vec{\nabla} = \left(\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right)$$

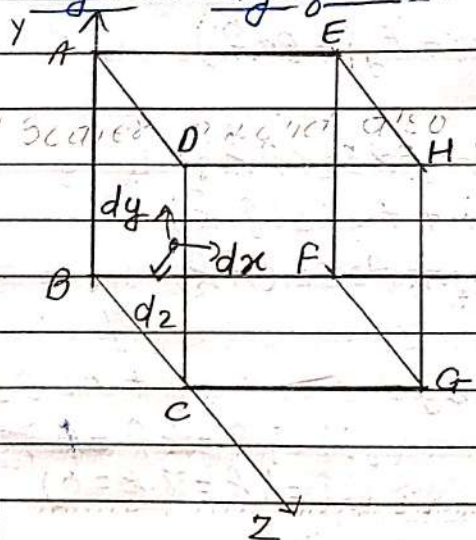
$$\text{& } \vec{v} = (v_x \hat{i} + v_y \hat{j} + v_z \hat{k})$$

$$13 \therefore \vec{\nabla} \cdot \vec{v} = \left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} \right)$$

- 14 Also, $\vec{\nabla} \cdot \vec{v}$ is a scalar function.



* Physical Significance.



1] Consider a rectangular parallelepiped ABCD-EFGH on co-ordinate system

x, y, z

2] Let dx, dy & dz be lengths of parallelepiped & v_x, v_y & v_z be a vector entering thr ABCD.

3] When a vector enters through ABCD, then
 $= v_x dy dz$ — (1)

when it leaves from EFGH, then

$$= v_x dy dz - \frac{\partial v_x}{\partial x} dx dy dz \text{ — (2)}$$

$\therefore$ Net flux from parallelepiped through x-axis
 $(2) - (1)$

$$= v_x dy dz - v_x dy dz + \frac{\partial v_x}{\partial x} dx dy dz$$

$$= \frac{\partial v_x}{\partial x} dx dy dz \text{ — (3)}$$

4] Similarly, the net vector form y axis is
 $= \frac{\partial v_y}{\partial y} dx dy dz \text{ — (4)}$

And from z,

$$= \frac{\partial v_z}{\partial z} dx dy dz \text{ — (5)}$$

5] $\therefore$ from (3) (4) (5).

$$\nabla \cdot \vec{v} = \left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} \right) dx \cdot dy \cdot dz$$



Sai S. Ivare

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- शिक्षणमहर्षी डॉ. बापूजी साबुंखे

Shri Swami Vivekanand Shikshan Sanstha Kolhapur's

51486

VIVEKANAND COLLEGE, KOLHAPUR (AUTONOMOUS)

SUPPLIMENT

Suppliment No. : (1)

Roll No. : 7253

Class : BSc (I)

Signature
of
Supervisor

Subject : Physics

Test / Tutorial No. :

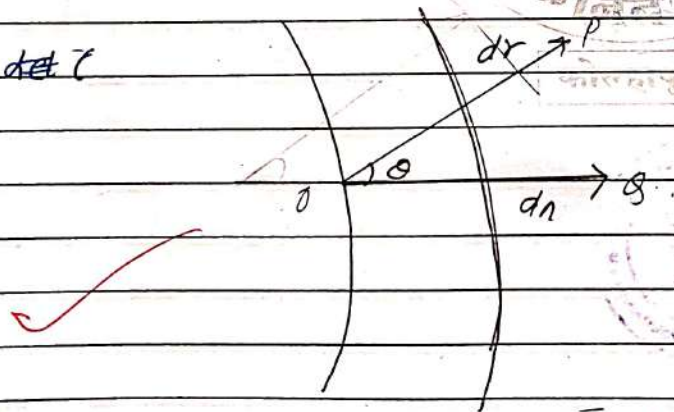
Div. :

Q Therefore, divergence per unit volume is

$$\nabla \cdot \vec{v} = \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z}$$

2) Physical significance of gradient of scalar function

Q det



$$\cos \theta = \frac{dn}{dr}, \quad dn = dr \cos \theta$$



Q consider a del operator $\vec{\nabla}$ & scalar function ϕ such that

$$\vec{\nabla} = \frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \quad \& \quad \phi = \phi_x \hat{i} + \phi_y \hat{j} + \phi_z \hat{k}$$

Q Therefore their dot product is taken as

$$\vec{\nabla} \cdot \phi = \left(\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) \cdot (\phi_x \hat{i} + \phi_y \hat{j} + \phi_z \hat{k}) \quad \text{do}$$

$$\vec{\nabla} \cdot \phi = \left(\frac{\partial \phi}{\partial x} \hat{i} + \frac{\partial \phi}{\partial y} \hat{j} + \frac{\partial \phi}{\partial z} \hat{k} \right) \quad (\text{This is called grad of scalar field}).$$

Also, if $dr = dx\hat{i} + dy\hat{j} + dz\hat{k}$ & $\cos\theta = \cos 0 = 1$

Then it becomes,

$$\vec{\nabla} \cdot \phi = \left(\frac{\partial \phi}{\partial x} dx + \frac{\partial \phi}{\partial y} dy + \frac{\partial \phi}{\partial z} dz \right) (\hat{i} + \hat{j} + \hat{k})$$

$$\vec{\nabla} \cdot \phi = \left(\frac{\partial \phi}{\partial x} dx + \frac{\partial \phi}{\partial y} dy + \frac{\partial \phi}{\partial z} dz \right)$$

Therefore this is called gradient of scalar field which can also be written as

$$\vec{\nabla} \cdot \phi = \frac{\partial \phi}{\partial x} + \frac{\partial \phi}{\partial y} + \frac{\partial \phi}{\partial z}$$

It is a vector function.



॥ ज्ञान, विज्ञान आणि सुसंस्कार यांसाठी शिक्षण प्रसार ॥

- शिक्षणमहर्षी डॉ. बापूजी साळुंखे

Shri Swami Vivekanand Shikshan Sanstha Kolhapur's

51474

VIVEKANAND COLLEGE, KOLHAPUR (AUTONOMOUS)

SUPPLIMENT

Name : Megha Sambhaji Patil

Suppliment No. : 01

Roll No. : 7223

Class : B.S.C I

Signature
of
Supervisor

Subject : physics

Test / Tutorial No. :

Div. :

10
10 *July*

Q1) The gradient of scalar function ($\nabla \phi$) is vector

2) If magnitude of $\vec{A} \times \vec{B} = AB$, then two vectors must be antiparallel to each other

Q2) Scalar product :- If two vectors, inclined at some angle θ , then their ^{scalar} ~~cross~~ product will be product of their magnitudes and cosine angle between them

$$\vec{V} = \vec{A} \cdot \vec{B}$$

$$= |\vec{A}| |\vec{B}| \cos \theta$$

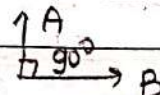
* characteristics

(1) Scalar product holds commutative law
i.e. $\vec{A} \cdot \vec{B} = \vec{B} \cdot \vec{A}$

(2) Scalar product holds distributive law
 $\vec{A} \cdot (\vec{B} + \vec{C}) = \vec{A} \cdot \vec{B} + \vec{A} \cdot \vec{C}$

(3) IF two vectors are parallel to each other
 angle, $\theta = 0^\circ$
 $\cos 0^\circ = 1$

(4) IF two vectors are perpendicular to each other
then the angle; $\theta = 90^\circ$
 $\cos(90^\circ) = 0$



⑤ IF two vectors are antiparallel then,

$$\theta = 180^\circ$$

$$\cos(180^\circ) = -1$$

we get negative sign here

⑥ one of the well known example of scalar product is work done

$$\text{Work done} = \text{Force} \cdot \text{displacement}$$
$$W = F \cdot ds$$

Q2) Let ϕ be the scalar Function, then the quantity $\left(\frac{\partial \phi}{\partial x} \hat{i} + \frac{\partial \phi}{\partial y} \hat{j} + \frac{\partial \phi}{\partial z} \hat{k} \right)$ is a gradient of scalar Function ϕ is called as grad ϕ .

Denoted by the symbol $\nabla \phi$ or grad ϕ . here ϕ is continuously differentiable Function.

$$\text{grad } \phi = \frac{\partial \phi}{\partial x} \hat{i} + \frac{\partial \phi}{\partial y} \hat{j} + \frac{\partial \phi}{\partial z} \hat{k}$$

$$\text{let } \phi = \phi(x, y, z)$$
$$= \phi(r)$$

$$= \text{here } r = x\hat{i} + y\hat{j} + z\hat{k}$$



IF $d\phi =$

$$d\phi = dx\hat{i} + dy\hat{j} + dz\hat{k} \text{ then total differential}$$
$$\text{Function } d\phi = \frac{\partial \phi}{\partial x} dx + \frac{\partial \phi}{\partial y} dy + \frac{\partial \phi}{\partial z} dz$$

here $\nabla =$ del operator, which is vector differential operator.

$$\text{denoted by } \nabla = \hat{i} \frac{\partial}{\partial x} + \hat{j} \frac{\partial}{\partial y} + \hat{k} \frac{\partial}{\partial z}$$

which is used, in gr

It gives total variation of Field (scalar or

ector) and give maximum rate of change of that field. It act as simple differentiator, which operates on scalar function ϕ .

$\vec{\nabla} \cdot \phi$:- here $\vec{\nabla}$ operates on scalar function ϕ .
 $\vec{\nabla} \cdot \vec{v}$ & $\vec{\nabla} \times \vec{v}$ is a formal vector.

here scalar field define as :- when we give scalar quantity to every point in space, it is called as scalar field.

eg of scalar field :- electric potential
magnetic potential
gravitational potential.

3) Vector Field :- when vector quantity is given to every point in space, it is called as vector field.

Let $\vec{v}(x, y, z)$ be the continuous differentiable function, then the quantity

$\left[\hat{i} \frac{\partial \vec{v}}{\partial x} + \hat{j} \frac{\partial \vec{v}}{\partial y} + \hat{k} \frac{\partial \vec{v}}{\partial z} \right]$ is a divergence

of vector field, denoted by $\vec{\nabla} \cdot \vec{v}$.

let $\vec{v} = v_x \hat{i} + v_y \hat{j} + v_z \hat{k}$
then

divergence of vector field

can be written as

$$\vec{\nabla} \cdot \vec{v} = \left(\hat{i} \frac{\partial}{\partial x} + \hat{j} \frac{\partial}{\partial y} + \hat{k} \frac{\partial}{\partial z} \right) \cdot (v_x \hat{i} + v_y \hat{j} + v_z \hat{k})$$
$$= \left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} \right) = \text{Divergence}$$

of vector field.

This is scalar quantity.



Divergence can also be defined as
Total Flux diverging per unit volume of a
vector element of a vector field.

Total Flux of vector element,
$$\left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} \right) \cdot dx \cdot dy \cdot dz$$

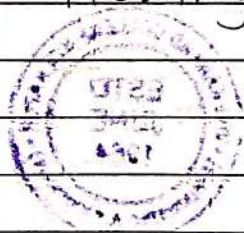
here $dx \cdot dy \cdot dz$ is volume,

So, Total Flux per unit volume,

$$\left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} \right) \cdot dx \cdot dy \cdot dz$$

here, above terms get cancel out,
we get the divergence.

Divergence used in hydrodynamics,
it represents the rate at which fluid is
flowing.



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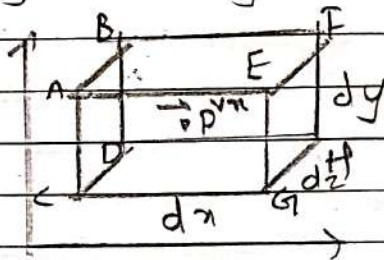
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3) physical significance:



Consider a rectangular parallelepiped ABCDEFGH having sides dx, dy, dz parallel to the axes.

Let velocity of the fluid v at the centre, $v(v_x, v_y, v_z)$. The field of vector changes from point to point. ~~It~~ Divergence is used to measure how vector is spread from point to point.

The component of x of its magnitude is

$(v_x - \frac{\partial v_x}{\partial x} \cdot \frac{dx}{2})$ normally inwards

$(v_x + \frac{\partial v_x}{\partial x} \cdot \frac{dx}{2})$ normally outwards

Total Flux, $d\phi = \vec{v} \cdot d\vec{s}$
 $\vec{v} \cdot dydz$

$[(\frac{\partial v_x}{\partial x}) dydz \text{ along } x \text{ component}]$



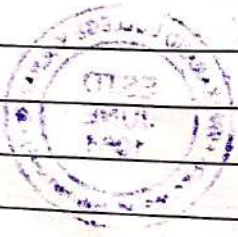
Total Flux along all the axes

$$\left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} \right) dx dy dz$$

(2)



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Q.1)

1)

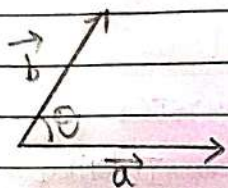
07 the gradient of scalar function ($\nabla \phi$) is a scalar and used to represent equipotential surface.

2) If magnitude of $\vec{A} \times \vec{B} = AB$ then two vectors must be parallel to each other inclined at an angle 45° with each other.



Q.2.

1) scalar product:



Let $\vec{a}$ and $\vec{b}$ are two vectors inclined each other at an angle θ .

Then the scalar product of two vectors is product of magnitude of given two vectors i.e. $\vec{a}$ and $\vec{b}$ and cosine of the angle betⁿ them.

$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta$$

characteristics of scalar product:

1) The scalar product obey commutative law.
i.e. $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{a}$

2) The scalar product distributive over vector addition.

Let $\vec{a}$, $\vec{b}$ and $\vec{c}$ are three vectors

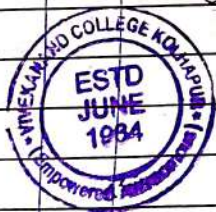
$$\vec{a} \cdot (\vec{b} + \vec{c}) = \vec{a} \cdot \vec{b} + \vec{a} \cdot \vec{c}$$

3) When two vectors are parallel to each other then their scalar product is maximum.

$$\theta = 0 \quad \text{or} \quad \theta = 180^\circ$$

$$\vec{a} \cdot \vec{b} = ab \cos \theta$$

$$= ab \cos 0^\circ$$



i.e. $\cos 0^\circ = 1$

$$\therefore \vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}|$$

4) When the two vectors are perpendicular to each other, then their scalar product becomes zero.

$$\cos 90^\circ = 0$$

$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos 90^\circ$$

$$= \underline{\underline{0}}$$

5) In case of orthogonal vectors

$$\hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1$$

where $\hat{i}, \hat{j}, \hat{k}$ are mutually parallel to each other.

6) let $\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$

$$\vec{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$$

$$\therefore \vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z$$

if $\vec{A} = \vec{B}$

$$\vec{A} \cdot \vec{A} = A^2$$

$$\vec{A} \cdot \vec{A} = A_x^2 + A_y^2 + A_z^2$$



3)

divergence of vector field: $(\vec{\nabla} \cdot \vec{v})$

$$\frac{\partial v_x}{\partial x} \hat{i} + \frac{\partial v_y}{\partial y} \hat{j} + \frac{\partial v_z}{\partial z} \hat{k}$$

The $v(x, y, z)$ is the continuous differential vector function and $\frac{\partial v_x}{\partial x} \hat{i} + \frac{\partial v_y}{\partial y} \hat{j} + \frac{\partial v_z}{\partial z} \hat{k}$ is called as divergence of vector field

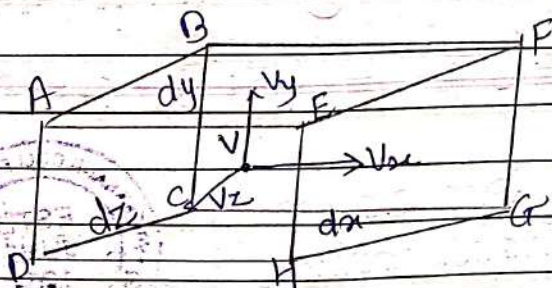
$$\text{As } \vec{\nabla} = \text{gradient } \frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k}$$

$$\text{and } \vec{v}(x, y, z) = v(\vec{r}) \\ = v_x \hat{i} + v_y \hat{j} + v_z \hat{k}$$

$$\therefore \vec{\nabla} \cdot \vec{v} = \left(\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) \cdot (v_x \hat{i} + v_y \hat{j} + v_z \hat{k})$$

$$\therefore \vec{\nabla} \cdot \vec{v} = \frac{\partial v_x}{\partial x} \hat{i} + \frac{\partial v_y}{\partial y} \hat{j} + \frac{\partial v_z}{\partial z} \hat{k}$$

Thus the divergence of vector field is a product of gradient and vector function denoted by $\vec{\nabla} \cdot \vec{v}$.



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physical significance of vector field.

Consider a parallelepiped ABCD-EFGH. having length dx, dy, dz .

Let $\vec{r} = vx\hat{i} + vy\hat{j} + vz\hat{k}$ which is the point on centre of parallelepiped.

The vector ^{field} changes from point to point. |

vector field: The quantity assigned to every point in space is called vector field.

- The vector field is a scalar quantity.



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Department of Physics

B.Sc. Part-I SEM I Examination (2024-25)
Mechanics I

Paper I (Paper code: DSC03PHY11)

Date :
Day :

Total Marks: 10
Time :-

Instructions:-

- 1) All questions are compulsory.
- 2) Figures to the right indicate full marks.
- 3) Use of log table and calculator is allowed.

Q.1) Select correct alternative

(2)

1. Angular momentum is conserved when there is ----- net torque applied to a system.
(a) zero (b) infinity
(c) one (d) none of above
2. The energy conservation theorem states that the total energy of a particle in a conservative force field is -----.
(a) zero (b) constant
(c) infinity (d) one

Q.2) Attempt any TWO

(08)

1. State and explain conservation theorem of angular momentum for a particle.
2. Define and explain the physical significance of Center of mass.
3. State and explain conservation theorem of linear momentum for system particles.



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Q1)

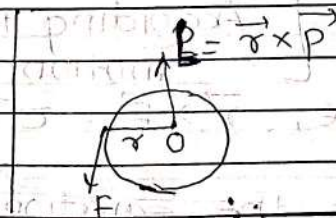
1) Angular momentum is conserved when there is zero net torque applied to a system.

2) The energy conservation theorem states that the total energy of a particle in a conservative force field is constant.

Q2) ①

Statement:- when the torque applied to a particle is zero then, angular momentum is conserved.

Diagram



Let consider a particle of mass m , moving about point O .

② Let r be the position vector about point O

③ Let L be the angular momentum about point O

$$\text{i.e. } L = \vec{r} \times \vec{p} \quad \text{--- (1)}$$

p is here linear momentum of that particle.
if we take rate of change of equation on both side w.r.t time.

$$\text{i.e. } \frac{dL}{dt} = \frac{d(\vec{r} \times \vec{p})}{dt}$$

$$= \frac{d(\vec{r} \times \vec{p})}{dt}$$

$$= \vec{r} \times \frac{d\vec{p}}{dt} + \frac{d\vec{r}}{dt} \times \vec{p}$$

$$= \vec{r} \times \frac{d\vec{p}}{dt} + \frac{d\vec{r}}{dt} \times m\vec{v} \quad \left[\begin{array}{l} \text{Linear momentum} \\ \text{is product of} \\ \text{mass and} \end{array} \right.$$

$$= \vec{r} \times \frac{d\vec{p}}{dt} + \vec{v} \times m\vec{v} \quad \left[\begin{array}{l} \text{velocity} \\ \text{rate of change} \\ \text{of } \vec{r} \text{ w.r.t time} \\ \text{is } \vec{v}. \text{ i.e. } \frac{d\vec{r}}{dt} \end{array} \right.$$

Here $\vec{v} \times m\vec{v} = 0$, because
Cross product of vector to itself is zero

$$= \vec{r} \times \frac{d\vec{p}}{dt}$$

$$= \vec{r} \times \frac{d\vec{p}}{dt} \text{ is written as } \tau$$

$$= \vec{r} \times \vec{F} \quad \left[\begin{array}{l} \text{According to 2nd Law of} \\ \text{motion} \end{array} \right] \therefore$$

$$= \text{because, } \vec{r} \times \vec{F} = \tau \quad (\text{definition of torque})$$

So, we can write the equation as

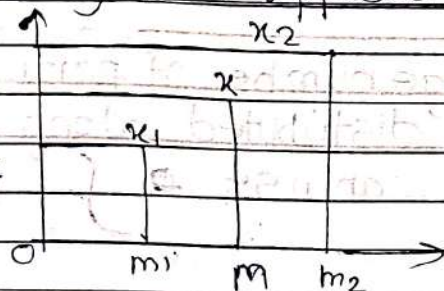
$$\frac{dL}{dt} = \tau$$

If $\tau = 0$, then $\frac{dL}{dt} = 0$, i.e. $L = \text{constant}$



hence, angular momentum is conserved.

2] centre of mass:- COM is the point, where whole mass of body is supposed to be concentrated.



Let m_1, m_2 are the point masses w.r.t origin at a distance x_1, x_2 , here total mass M is at a distance x .

By equating mass-moment about origin, we can write

$$(m_1 + m_2) x_{cm} = m_1 x_1 + m_2 x_2$$

$$\therefore x_{cm} = \frac{m_1 x_1 + m_2 x_2}{m_1 + m_2} \quad \text{--- (1)}$$

If there are 'n' number of particles present along the centre of mass, then eqn (1) become,

$$x_{cm} = \frac{m_1 x_1 + m_2 x_2 + \dots + m_n x_n}{m_1 + m_2 + \dots + m_n} = \frac{\sum_{i=1}^n m_i x_i}{M}$$

If we want to describe the above equation in 3-d space, then centre of mass about origin can be denoted with the help of coordinate (x, y, z)

$$\text{i.e. } x_{cm} = \frac{\sum_{i=1}^n m_i x_i}{M}$$

$$y_{cm} = \frac{\sum_{i=1}^n m_i y_i}{M}$$

$$z_{cm} = \frac{\sum_{i=1}^n m_i z_i}{M}$$



All these 3 equation can be combine using vector notation r ,

i.e $r_{cm} = x_{cm}\hat{i} + y_{cm}\hat{j} + z_{cm}\hat{k}$

If there are large number of particles present, which are uniformly distributed along centre of mass, then we can use $\int$ for the

Σ

$$r_{cm} = \frac{\int m_i r_i}{\int dm} = \frac{\int m_i r_i}{M} \quad \text{--- (ii)}$$

So, Let consider, 'n' no. of particles present having mass $m_1, m_2, m_3, \dots, m_n$, here 'no' particle can leave the system, i.e Mass is constant here.

From (i) we can write,

$$M r_{cm} = m_1 r_1 + m_2 r_2 + m_3 r_3 + \dots + m_n r_n$$

From eqn (ii)

but if we differentiate the above equation we get

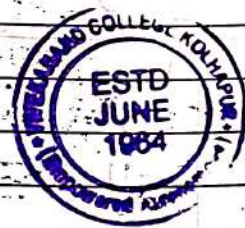
$$M \frac{dr}{dt} = m_1 \frac{dr_1}{dt} + \dots + m_n \frac{dr_n}{dt} \quad ; \quad \text{i.e.}$$

$$\text{but } \frac{dr}{dt} = v$$

$$M v_{cm} = m_1 v_1 + \dots + m_n v_n$$

again if we differentiate we get

$$M \frac{dv}{dt} = m_1 \frac{dv_1}{dt} + m_2 \frac{dv_2}{dt} + \dots + m_n \frac{dv_n}{dt}$$



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Q2. $\frac{dv}{dt} = a$

So we can write equation of

$$m \cdot a = m_1 a_1 + m_2 a_2 + \dots + m_n a_n$$

From using Newton second equation

$$m \cdot a = F$$

BUT here force is external because, internal force is cancel, because they are equal and opposite in the direction.

Q3] Statement:- IF force acting on system of particles is zero, then linear momentum of system of particles is conserved.

Diagram



Let consider, there are N number of particles consider the i-th particle of the system

Force acting on i^{th} particle, can be written as

$$F_i = F_i(e) + \sum_{j=1}^N F_{ij} \quad \text{--- (1)}$$

external
force

internal
force

F_{ij} which acts on the j^{th} particle.

$$F_i = \frac{dp_i}{dt} \quad \text{--- [Newton's second law of motion,]}$$

eqn (1) becomes

$$\frac{dp_i}{dt} = F_i(e) + \sum_{j=1}^N F_{ij} \rightarrow \text{For } i^{\text{th}} \text{ particle}$$

for whole system take summation on the both side

$$\sum_{i=1}^N \frac{dp_i}{dt} = \sum_{i=1}^N F_i(e) + \sum_{i=1}^N \sum_{j=1}^N F_{ij}$$

$$= \sum_{i=1}^N \frac{dp_i}{dt} = \sum_{i=1}^N F_i(e) + \sum_{i,j} F_{ij}$$

here F_{ij} become zero because, if force act on i^{th} then i^{th} particle also act on the other particle. i.e they all are equal and opposite, so all internal force get cancel.

$$\sum_{i=1}^N \frac{dp_i}{dt} = \sum_{i=1}^N F_i(e)$$

$$\frac{dp}{dt} = F(e)$$

if $F_i(e) = 0$ then $\frac{dp}{dt} = 0$

hence $p = \text{constant}$



hence linear momentum is conserved for system of particles.



Name :- Harshvardhan. M. Kate

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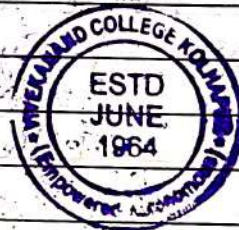
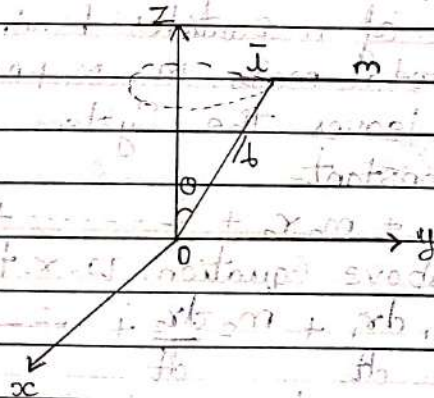
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Q1] 1] Angular momentum is conserved when there is Zero net torque applied to a system.

2] The energy conservation theorem states that total energy of a particle in a conservative force field is constant.

Q2] 1]



Consider a particle moving with mass 'm' with torque τ . Let $\vec{p}$ be the linear momentum of the particle and $\vec{r}$ be its position vector.

$$\therefore \text{The } \vec{L} = \vec{r} \times \vec{p} \quad \text{--- (1)}$$

But τ is perpendicular to a plane $\vec{r}$ and $\vec{p}$

$$|\vec{L}| = r p \sin \alpha \quad \text{--- where } r \sin \alpha \text{ is component } \vec{r} \text{ which is } \perp \text{ to } \vec{p}$$

$$\therefore \text{For single particle } \vec{F} = \frac{d\vec{p}}{dt} \quad \text{--- (2)}$$

Differentiating eqⁿ ① with respect to time.

$$\frac{d\vec{L}}{dt} = \vec{r} \times \frac{d\vec{p}}{dt} + \vec{p} \times \frac{d\vec{r}}{dt}$$

$$= \vec{r} \times \frac{d\vec{p}}{dt} + m\vec{v} \times \vec{v}$$

$$= \vec{r} \times \frac{d\vec{p}}{dt} + 0$$

$$= \vec{r} \times \frac{d\vec{p}}{dt} \quad \text{--- ③}$$

∴ After comparing eqⁿ ② & ③

$$\frac{d\vec{L}}{dt} = 0$$

✓ The rate of change of momentum is equal to the torque acting on it.

If net torque acting on a particle is zero then $\frac{d\vec{L}}{dt} = 0$

∴ The angular momentum of a particle is conserved.

2) → Consider a system of n particles having masses $m_1, m_2, \dots, m_n$ and total mass $M = m_1 + m_2 + \dots + m_n$

No particle enters or leaves the system as the total mass of system is constant.

$$\therefore \vec{r}_{cm} = m_1 \vec{r}_1 + m_2 \vec{r}_2 + \dots + m_n \vec{r}_n$$

Differentiating above equation w.r.t time

$$\frac{d\vec{r}_{cm}}{dt} = m_1 \frac{d\vec{r}_1}{dt} + m_2 \frac{d\vec{r}_2}{dt} + \dots + m_n \frac{d\vec{r}_n}{dt}$$

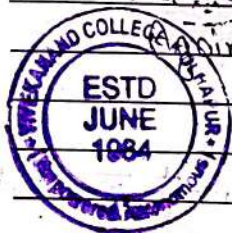
But $\vec{v}_{cm} = \frac{d\vec{r}_{cm}}{dt}$ = velocity of centre of mass

$$\vec{v}_{cm} = m_1 \vec{v}_1 + m_2 \vec{v}_2 + \dots + m_n \vec{v}_n$$

again differentiating with respect to time

$$\frac{d\vec{v}_{cm}}{dt} = m_1 \frac{d\vec{v}_1}{dt} + m_2 \frac{d\vec{v}_2}{dt} + \dots + m_n \frac{d\vec{v}_n}{dt}$$

$$\text{But } \vec{a}_{cm} = \frac{d\vec{v}_{cm}}{dt}$$



$$\therefore a_{cm} = m_1 a_1 + m_2 a_2 + \dots + m_n a_n$$

There are two internal forces acting on a particle internal as well as external. But internal forces are equal and opposite so they cancel. There exists only external force on a particle.

Acc to Newton's Second law

$$F = F_{ext}$$

$$= F_1 + F_2 + \dots + F_n$$

3) Thus the total energy of mass centre of mass is the mass of

3) Consider a system of n particles having masses $m_1, m_2, \dots, m_n$ & velocity $v_1, v_2, \dots, v_n$. Assume that no. of particles enters and leaves the system so that total part of the system is constant.

The total mass of a system is vector sum of individual particle. i.e.

$$F = F_{ext}$$

$$= F_1 + F_2 + \dots + F_n$$

Let $\vec{P}_1, \vec{P}_2, \dots, \vec{P}_n$ be the linear momentum of a system of particle where $P = mv$

The total momentum of particle system particle is given as

$$\vec{P} = \vec{P}_1 + \vec{P}_2 + \dots + \vec{P}_n$$

$$mv = m_1 v_1 + m_2 v_2 + \dots + m_n v_n$$

According to Newton's Second law

$$F = ma$$

$$= m \frac{dv}{dt}$$

$$F = \frac{d\vec{P}}{dt}$$

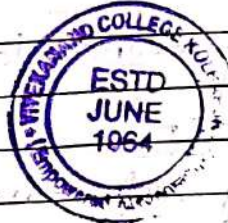
$\therefore$ If the net force acting on the system of particle

is zero then $\frac{d\vec{P}}{dt} = 0$

$\therefore P = \text{constant}$



i. The vector sum of moment of all particles in a system remains constant if the resultant force acting on system is zero.



Let us consider a system of particles. Let the total external force acting on the system be zero. Then the total momentum of the system is conserved. This is because the rate of change of total momentum is equal to the total external force. If this force is zero, the total momentum remains constant.

Let the particles have masses $m_1, m_2, \dots, m_n$ and velocities $\vec{v}_1, \vec{v}_2, \dots, \vec{v}_n$. The total momentum $\vec{P}$ is given by:

$$\vec{P} = m_1 \vec{v}_1 + m_2 \vec{v}_2 + \dots + m_n \vec{v}_n$$

According to Newton's second law, the rate of change of momentum is equal to the net force. If the net force is zero, the total momentum is constant. This can be written as:

$$\frac{d\vec{P}}{dt} = 0$$

$$\vec{P} = \text{constant}$$

Thus, the vector sum of the moment of all particles in a system remains constant if the resultant force acting on the system is zero.

“ ज्ञान, विज्ञान आणि सुसंस्कार यांसाठी शिक्षण प्रसार ”

-शिक्षणमहर्षी डॉ. बापूजी साळुंखे

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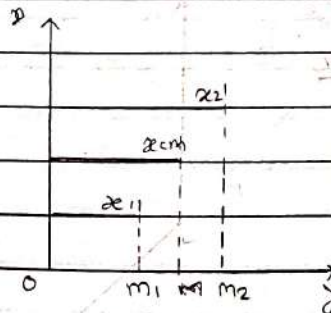
Q.1.

1) a) zero.

2) b) constant.

Q.2.

2/1)



We have, in fig.

$$(m_1 + m_2)2cm = m_1x_1 + m_2x_2$$

$$2cm = \frac{m_1x_1 + m_2x_2}{m_1 + m_2}$$

Consider, a'n particles of masses $m_1, m_2, m_3, \dots, m_n$ having total mass $M = m_1 + m_2 + m_3 + \dots + m_n$

Defⁿ:-

"Centre of mass is a point where the ~~the~~ mass of whole body is concentrated."

$$\therefore M = m_1 + m_2 + m_3 \dots m_n \quad \text{with } r$$

$\therefore$ the vector

$$M = m_1 \vec{r}_1 + m_2 \vec{r}_2 + m_3 \vec{r}_3 + \dots + m_n \vec{r}_n$$

differentiating with time

$$M = m_1 \frac{d\vec{r}_1}{dt} + m_2 \frac{d\vec{r}_2}{dt} + m_3 \frac{d\vec{r}_3}{dt} \dots + m_n \frac{d\vec{r}_n}{dt}$$

$$\therefore M = \frac{\sum m_i \vec{r}_i}{\sum m_i}$$

from



3)

→ Consider s: 'n' no. of particles in a system with linear momentum $\vec{P}$.

$$\vec{P} = \vec{P}_1 + \vec{P}_2 + \vec{P}_3$$

m is the mass & v be the velocity of those particles.

We have,

$$\vec{P} = \vec{m} \times \vec{v}$$

• If the external force acting on a system is zero, then the linear momentum said to be conserved.

• If external force is zero,

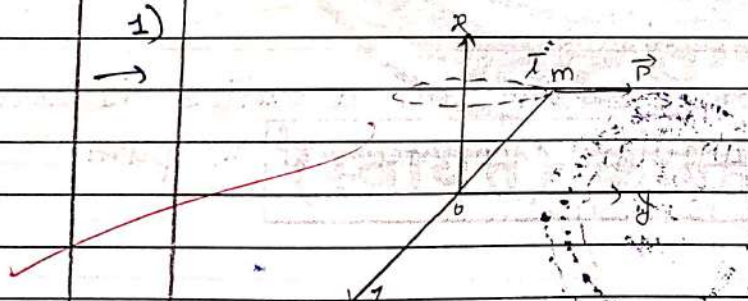
$$\therefore \vec{P} \frac{d\vec{P}}{dt} = 0$$

$$\therefore \vec{P} = \text{constant.}$$



1)

→



Consider a particle of mass 'm' rotating about its axis with Torque 'T'.

$\vec{P}$ be the linear momentum & $\vec{r}$ be the radius of its rotation.

We know,

$$\vec{P} = m\vec{v}$$

$\vec{L}$ is the angular momentum of the particle

$$\therefore \vec{L} = \vec{P} \times \vec{r} \text{ --- (1)}$$

$$\vec{L} = pr \sin \theta$$

where, $pr \sin \theta$ is a component of r .

We take ^{torque} force of one particle,

Diff. eqⁿ ① with t

$$\frac{d\vec{L}}{dt} = r \left(\frac{d\vec{p}}{dt} \right) + \left(\frac{d\vec{r}}{dt} \right) \times \vec{p}$$

$$\frac{d\vec{L}}{dt} = \vec{r} \times \frac{d\vec{p}}{dt} + \vec{p} \times m \cdot \vec{v}$$

$$\frac{d\vec{L}}{dt} = \vec{r} \times \frac{d\vec{p}}{dt} \quad [\because m\vec{v} = \vec{p}]$$

Therefore, i) angular momentum of a particle in a system is equal to the torque.

ii) If the torque acting on particle is zero, then $\frac{d\vec{L}}{dt} = 0$

$$\vec{L} = \text{constant.}$$

iii) If the torque acting on a particle is zero, then the angular momentum of a particle in a system is conserved.

